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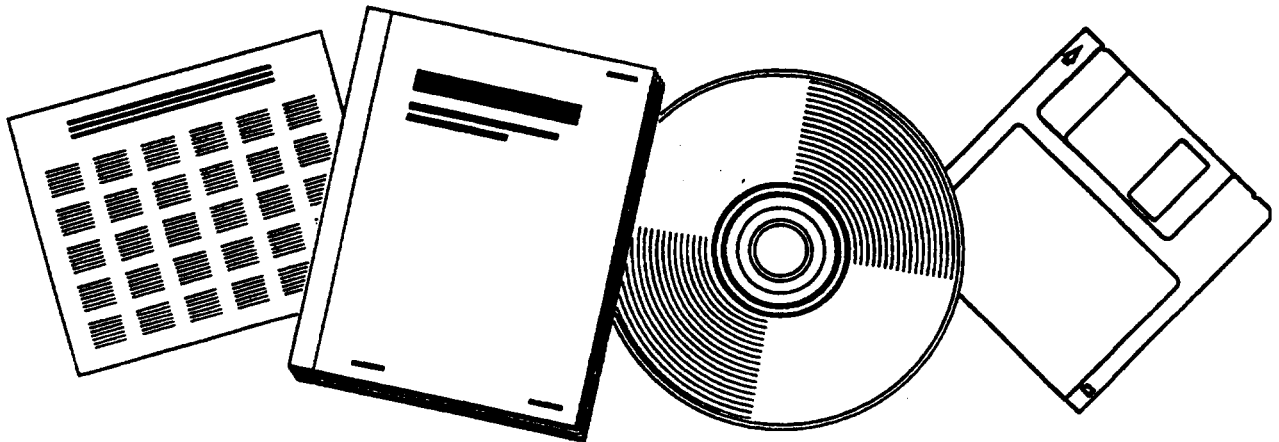
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# HYDRODYNAMICS OF THE THREE-PHASE SLURRY FISCHER-TROPSCH BUBBLE COLUMN REACTORS. FINAL REPORT

TEXAS A AND M UNIV., COLLEGE STATION.  
DEPT. OF CHEMICAL ENGINEERING

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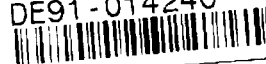


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**HYDRODYNAMICS OF THREE-PHASE SLURRY FISCHER-TROPSCH BUBBLE  
COLUMN REACTORS**

**Final Report**

**By**  
**Dragomir B. Bukur**  
**James G. Daly**  
**Snehal A. Patel**

**September 1990**

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**For**  
**U.S. Department of Energy**  
**Pittsburgh Energy Technology Center**  
**Pittsburgh, Pennsylvania**

**By**  
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HYDRODYNAMICS OF THREE-PHASE SLURRY  
FISCHER-TROPSCH BUBBLE COLUMN REACTORS

FINAL REPORT

DRAGOMIR B. BUKUR, JAMES G. DALY AND SNEHAL A. PATEL

TEXAS A&M UNIVERSITY  
DEPARTMENT OF CHEMICAL ENGINEERING  
COLLEGE STATION, TX 77843

September 1990

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George Cinquegrane, Project Manager (PETC)

John Shen, Program Manager (DOE/FE)

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