

VII. NOMENCLATURE

- a_s = specific gas-liquid interfacial area, m^2 / m^3
 A_i = atomic mass of species i , Chapter III, $kg/kmole$
 Ar = Archimedes number
 A_L = cross sectional area of the column occupied by large bubbles, m^2
 A_s = cross sectional area of the column occupied by small bubbles, m^2
 A_{s_i} = area of region i , defined by Eq. 3.39, m^2
 A_x = cross sectional area of the column, m^2
 A_x = cross sectional area of the absorbing media, Chapter III, m^2
 a = slope of pressure transducer calibration curve, inches water/volts
 b = intercept of pressure transducer calibration curve, inches water
 Bo = Bond number
 B = number of photons crossing a unit area per unit time
 B_o = incident number of photons crossing a unit area per unit time
 B_i = number of photons crossing a unit area per unit time
 for source i
 B_{oi} = incident number of photons crossing a unit area per unit
 time for source i
 C_s = solids concentration, kg/m^3
 C_s^B = solids concentration at the bottom of the dispersion, kg/m^3
 C_s^f = solids concentration in the feed, kg/m^3
 d = distance through the column, m
 d_{Bi} = size of bubble i , m
 d_c = column diameter, m
 d_{col} = column diameter, m
 d_i = distance through the column at position i , m

- d_p = particle diameter, m
 d_s = Sauter mean bubble diameter, m
 E_s = axial dispersion coefficient, m^2/s
 $f_{d_{ij}}$ = volume fraction of the dispersion between pressure ports i and j
 f_{o_i} = fraction of the incident beam passing through phase i
 Fr_g = Froude number = $\frac{ug}{\sqrt{gd_{col}}}$
 f_s = fraction of the cross sectional area occupied by small bubbles
 g = gravitational accelerational constant, $9.81 m/s^2$
 H_{DP} = height of the pressure transducer, m
 $H_t(t)$ = height of liquid above the presure transducer at time t, m
 $H_t(0)$ = height of liquid above the presure transducer at time t=0, m
 h = height, m
 h_s = static liquid height, m
 h_{exp} = expanded height, m
 I = intensity of radiation
 I_0 = initial intensity of radiation
 l_e = entry length, cm
 L = expanded height of the dispersion, m
MSE = mean square error, defined by Eq. 2.36
 m_{se} = weight of solidified slurry sample, kg
 m_1 = weight of structure + sample, kg
 m_2 = weight of structure + sample immersed in acetone, kg
 N = number of data points
 n_i = number of bubbles of size i
psd = power spectral density function
 P = pressure, inches water

- P = Fourier transform of the autocorrelation function
 \bar{P} = average pressure
 P_i = pressure
 P_n = probability associated with a Poisson process, defined by Eq. 3.29
 Pe_p = particle Peclet number = $\frac{u_g d_{col}}{E_s}$
 r_c = column radius, m
 r_{pos_i} = radial position measured from the center of the column, defined by Eq. 3.38, m
 S_c = scale factor used in Eq. 3.34
 $s_{d_{ij}}$ = specific gravity of the dispersion between pressure ports i and j
 s_ℓ = specific gravity of the liquid
 $s_{s\ell_{ij}}$ = specific gravity of the slurry between pressure ports i and j
 Re_g = Reynolds number = $\frac{u_g d_{col} \rho_\ell}{\mu_\ell}$
 Re_p = particle Reynolds number = $\frac{u_T d_p \rho_\ell}{\mu_\ell}$
RMS = root mean square, defined by Eq. 6.2
 t = time, s
 u = lag
 u_{bs} = rise velocity of small bubbles, m/s
 u_{bL} = rise velocity of large bubbles, m/s
 u_g = superficial gas velocity, m/s
 u_ℓ = superficial liquid velocity, m/s
 u_p = hindered settling velocity of particles, m/s
 u_r = bubble rise velocity, Eq. 2.28, m/s
 $u_{s\ell}$ = superficial slurry velocity, m/s
 $u'_{s\ell} = \frac{u_{s\ell}}{(1-\epsilon_g)}$ in Eq. 4.3, m/s
 u_T = terminal rise velocity of a single particle in an infinite medium, m/s

- $V(t)$ = volume of liquid above the pressure transducer at time t , m^3
 V_i = volume of component i , defined by Eq. 3.11, m^3
 $V_L(t)$ = volume of large bubbles that rise above the pressure transducer at time t , m^3
 $V_{liq}(t)$ = volume of liquid displaced during Period I of disengagement, m^3
 V_o = volume of liquid above the pressure transducer at time $t=0$, m^3
 $V_\ell(t)$ = volume of the liquid entering the dispersion at time t , m^3
 V_{sl} = volume of solidified slurry, defined by Eq. 2.4, m^3
 $V_s(t)$ = volume of small bubbles that rise above the pressure transducer at time t , m^3
 V_T = total volume of the slurry, m^3
 V_{ij} = volume of the slurry in section ij , m^3
 w_i = weighting factor, defined by Eq. 3.40
 W_{acet} = weight of acetone displaced, defined by Eq. 2.3, kg
 We = Weber number, defined by Eq. 2.28
 x = dimensionless height above the distributor, Chapter IV, m
 x_i = thickness of species i , Chapter III, m
 Z_i = atomic number of species i , Chapter III

Greek Letters

- Δh_{ij} = height between pressure ports i and j , inches
 ΔI = change in intensity of radiation
 ΔP_{ij} = pressure drop across ports i and j , inches water
 Δt = time interval, sec
 Δx = thickness of the absorbing media, m
 ϵ_g = average gas holdup
 ϵ_{goL} = volume fraction of large bubbles at steady state
 ϵ_{goS} = volume fraction of small bubbles at steady state

ϵ_{gax} = axial gas holdup

ϵ_{gij} = gas holdup between pressure ports i and j

ϵ_l = average liquid holdup

ϵ_{lij} = liquid holdup between pressure ports i and j

ϵ_{meas} = measured gas holdup

ϵ_{pred} = predicted gas holdup

ϵ_{ri} = radial gas holdup at location i

ϵ_s = average solids holdup

ϵ_{sij} = solids holdup between pressure ports i and j

γ_{xx} = autocovariance function

κ_i = Compton scattering coefficient of component i, Chapter III, m^{-1}

μ = mean of the time series, Chapter IV

μ_l = liquid viscosity, Chapter II, kg/m-s

μ_{sl} = slurry viscosity, Chapter II, kg/m-s

μ_i = attenuation coefficient of species i, Chapter III, m^{-1}

μ_{ij} = attenuation coefficient of species i associated with source j, Chapter III, m^{-1}

ω_s = weight fraction of solids

ρ_i = density of the component i, kg/m^3

ρ_{acet} = density of acetone, kg/m^3

ρ_d = density of the dispersion, kg/m^3

ρ_g = density of the gas, kg/m^3

ρ_p = particle density, kg/m^3

ρ_s = density of solids, kg/m^3

ρ_{sl} = density of the solidified slurry, kg/m^3

ρ_w = density of solidified wax, kg/m^3

ρ_{water} = density of water, kg/m³

ρ_{xx} = autocorrelation function

σ_{ℓ} = surface tension of the liquid, N/m

σ_i = Compton scattering coefficient of component i, Chapter III, m⁻¹

τ_i = Compton scattering coefficient of component i, Chapter III, m⁻¹

Φ_{ℓ} = volume fraction of liquid in the slurry

$\overline{\Phi_{\ell}}$ = average volume fraction of liquid in the slurry

Subscripts

1,2,... = component number

g = gas

ℓ = liquid

s ℓ = slurry

s = solids

T = total

VIII. LITERATURE CITED

- Abou-el-Hassan, M.E., "A Generalized Bubble Rise Velocity Correlation," *Chem. Eng. Commun.*, **22**, 243 (1983)
- Abouelwafa, M.S.A., and E.J.M. Kendall, "The Measurement of Component Ratios in Multiphase Systems Using Gamma-Ray Attenuation," *J. Phys. E: Sci. Instrum.*, **13**, 341 (1980)
- Akagawa, K., H. Hamaguchi, and T. Sakaguchi, "I. Studies on the Fluctuation of Pressure Drop in Two-Phase Slug Flow," *Bulletin of JSME*, **14**, 447 (1971a)
- Akagawa, K., H. Hamaguchi, and T. Sakaguchi, "II. Studies on the Fluctuation of Pressure Drop in Two-Phase Slug Flow," *Bulletin of JSME*, **14**, 455 (1971b)
- Akagawa, K., H. Hamaguchi, and T. Sakaguchi, "III. Studies on the Fluctuation of Pressure Drop in Two-Phase Slug Flow," *Bulletin of JSME*, **14**, 462 (1971c)
- Akita, K., and F. Yoshida, "Bubble Size, Interfacial Area, and Liquid-Phase Mass Transfer Coefficient in Bubble Columns," *Ind. Eng. Chem. Proc. Des. Dev.*, **13**, 84 (1974)
- Albal, R.S., Y.T. Shah, N.L. Carr, and A.T. Bell, "Mass Transfer Coefficients and Solubilities for Hydrogen and Carbon Monoxide under Fischer-Tropsch Conditions," *Chem. Eng. Sci.*, **39**, 905 (1984)
- Attix, F.H., *Radiation Dosimetry, Volume I: Fundamentals*, Academic Press, New York (1968)
- Bach, H.F., and T. Pilhofer, "Variation of Gas Holdup in Bubble Columns with Physical Properties of Liquids and Operating Parameters of Columns," *Ger. Chem. Eng.*, **1**, 270 (1978)

- Badjugar, M.N., A. Deimling, B.I. Morsi, and Y.T. Shah, "Solids Distribution in a Batch Bubble Column," *Chem. Eng. Commun.*, **48**, 127 (1986)
- Bartholemew, R.N., and R.M. Casagrande, "Measuring Solids Concentrations in Fluidized Systems by Gamma-Ray Absorption," *Ind. Eng. Chem.*, **3**, 428 (1957)
- Basov V.A., V.I. Markheuka, T. Kh. Melik-Akhnazarov, and D.I. Orochko, "Investigation of the Structure of a Non-Uniform Fluidized Bed," *Int. Chem. Eng.*, **9**, 263 (1969)
- Baumgarten, P.K., and R.L. Pigford, "Density Fluctuations in Fluidized Beds," *AIChE J.*, **6**, 115 (1960)
- Bernatowicz, H., D. Gansmiller, and S. Wolff, "Final Report for the Development of a Three Phase Fraction Meter for Use at the SRC-1 Facility in Wilsonville, Alabama," Final Report to the Department of Energy for Contract Number DE-AC22-82PC50031 (1987)
- Bhatia, V.K., K.A. Evans, and N. Epstein, "Effect of Solids Wettability on Expansion of Gas-Liquid Fluidized Beds," *Ind. Eng. Chem. Proc. Des. Dev.*, **11**, 151 (1972)
- Buchholz, R., and K. Schugerl, "Bubble Column Bioreactors," *Europ. J. Appl. Micro.*, **6**, 301 (1979)
- Buchholz, R., J. Tsepetonides, J. Steinemann, and U. Onken, "Influence of Gas Distribution on Interfacial Area and Mass Transfer in Bubble Columns," *Ger. Chem. Eng.*, **6**, 105 (1983)
- Bukur, D.B., D. Petrovic, and J.G. Daly, "Hydrodynamics of Fischer-Tropsch Synthesis in Slurry Bubble Column Reactors," *Proc. DOE Indirect Liquefaction Contractors' Mtg.*, Houston, TX, 479 (1985)
- Bukur, D.B., and V.R. Kumar, "Effect of Catalyst Dispersion on Performance of Slurry Bubble Column Reactors," *Chem. Eng. Sci.*, **41**, 1435 (1986)

Bukur, D.B., J.G. Daly, S.A. Patel, M.L. Raphael, and G.B. Tatterson, "Hydrodynamics of Fischer-Tropsch Synthesis in Slurry Bubble Column Reactors," Final Report to the Department of Energy for Contract Number DE-AC22-84PC70027 (1987a)

Bukur, D.B., D. Petrovic, and J.G. Daly, "Flow Regime Transitions in a Bubble Column with a Paraffin Wax as the Liquid Medium," *Ind. Eng. Chem. Res.*, **26**, 1087 (1987b)

Bukur, D.B., S.A. Patel, and M.L. Raphael, "Hydrodynamic Studies in Fischer-Tropsch Derived Waxes in a Bubble Column," *Chem. Eng. Commun.*, **60**, 63 (1987c)

Bukur, D.B., and J.G. Daly, "Gas Hold-up in Bubble Columns for Fischer-Tropsch Synthesis," *Chem. Eng. Sci.*, **42**, 2967 (1987)

Calderbank, P.H., and M.B. Moo-Young, "The Continuous Phase Heat and Mass Transfer Properties of Dispersions," *Chem. Eng. Sci.*, **16**, 39 (1961)

Calderbank, P.H., F. Evans, R. Farley, G. Jepson, and A. Poll, "Rate Processes in the Catalyst-Slurry Fischer-Tropsch Reaction," *Catalysis in Practice - Instn. Chem. Engs.*, **66** (1963)

Chan, A.M.C., and S. Banerjee, "Design Aspects of Gamma Densitometers for Void Fraction Measurements in Small Scale Two-Phase Flows," *Nucl. Instr. Meth.*, **190**, 135 (1981)

Clift, R., J.R. Grace, and M.E. Weber, *Bubble Drops and Particles*, Academic Press, New York, 171, 236 (1978)

Cova, D.R., "Catalyst Suspension in Gas Agitated Tubular Reactors," *Ind. Eng. Chem. Proc. Des. Dev.*, **5**, 20 (1966)

Deckwer, W.D., Y. Louisi, A. Zaidi, and M. Ralek, "Hydrodynamic Properties of the

- Fischer-Tropsch Slurry Process," *Ind. Eng. Chem. Proc. Des. Dev.*, **19**, 699 (1980)
- Deimling, A., B.M. Karandikar, Y.T. Shah, and N.L. Carr, "Solubility and Mass Transfer of CO and H₂ in Fischer-Tropsch Liquids and Slurries," *Chem. Eng. J.*, **29**, 127 (1984)
- de Vries, R.J., W.P.M. Van Swaaij, C. Mantovani, and A. Heijkoop, "Design Criteria and Performance of the Commercial Reactor for the Shell Chlorine Process," *Proc. 5th Europ. Symp. Chem. Reaction Eng.*, Amsterdam, B9,59 (1972)
- El-Halwagi, M.M., and A. Gomezplata, "An Investigation of Solids Distribution Mixing, and Contacting Characteristics of Gas-Solid Fluidized Beds," *AIChE J.*, **13**, 503 (1967)
- Evans R.D., *The Atomic Nucleus*, McGraw-Hill, New York (1955)
- Fan, L.S., S. Satija, and K. Wisecarver, "Pressure Fluctuation Measurements and Flow Regime Transitions in Gas-Liquid-Solid Fluidized Beds," Paper 67E presented at AIChE Annual Meeting, San Francisco (1984).
- Fan, L.S., *Gas-Liquid-Solid Fluidization Engineering*, Butterworth Publishers, Stoneham, MA (1989)
- Fan, L.T., C.J. Lee, and R.C. Bailie, "Axial Solids Distribution in Gas-Solid Fluidized Beds," *AIChE J.*, **8**, 239 (1962)
- Fan, L.T., T.C. Ho, S. Hiraoka, and W.P. Walawender, "Pressure Fluctuations in a Fluidized Bed," *AIChE J.*, **27**, 388 (1981)
- Farley, R., and D.J. Ray, "Gamma Radiation Absorption Measurements of Density and Gas Holdup in a Three Phase Catalytic Reactor," *Brit. Chem. Eng.*, **9**, 830 (1964)

- Gibson, E.J., J. Rennie, and B.A. Say, "The Use of Gamma Radiation in the Study of the Expansion of Gas-Liquid Systems," *Int. J. of Appl. Rad. Iso.*, **2**, 129 (1957)
- Gidaspow D., C. Lin, and Y.C. Seo, "Fluidization in Two-Dimensional Beds with a Jet. 1: Experimental Porosity Distributions," *Ind. Eng. Chem. Fundam.*, **22**, 187 (1983)
- Glasgow, L.A., L.E. Erickson, C.H. Lee, and S.A. Patel, "Wall Pressure Fluctuations and Bubble Size Distributions at Several Positions in an Airlift Fermentor," *Chem. Eng. Commun.*, **29**, 34 (1984)
- Godbole, S.P., M.F. Honath, and Y.T. Shah, "Holdup Structure in Highly Viscous Newtonian and Non-Newtonian Solutions in Bubble Columns," *Chem. Eng. Commun.*, **16**, 119 (1982)
- Godbole, S.P., A. Schumpe, Y.T. Shah, and N.L. Carr, "Hydrodynamics and Mass Transfer in Non-Newtonian Solutions in a Bubble Column," *AIChE J.*, **30**, 213 (1984)
- Gray, D., M. Lytton, M. Neworth, and G. Tomlison, "The Impact of Developing Technology on Indirect Liquefaction," Final Report to the Department of Energy for Contract Number EF-77-C-01-2738 (1980)
- Gupte, K.M., J. Smith, T.M. Leib, and J.C.W. Kuo, "Fischer-Tropsch Bubble Column Hydrodynamics", *Proc. of the Fourth DOE Contractors' Conference on Indirect Liquefaction*, Washington, PA (1984)
- Hatate, Y., H. Nomura, T. Fujita, S. Tajiri, N. Hidaka, and A. Ikari, "Gas Holdup and Pressure Drop in Three-Phase Vertical Flows of Gas-Liquid-Fine Solid Particles System," *J. Chem. Eng. Jap.*, **19**, 56 (1986)
- Heijnen J.J, and K. Van't Riet, "Mass Transfer, Mixing and Heat Transfer Phenomena in Low Viscosity Bubble Column Reactors," *Chem. Eng. J.*, **28**, B21 (1984)

- Hughmark, G.A., "Holdup and Mass Transfer in Bubble Columns," *Ind. Eng. Chem. Proc. Des. Dev.*, **6**, 218 (1967)
- Ishigai, S., M. Yamane, and K. Roko, "Measurement of Component Flows in a Vertical Two-Phase Flow by Making Use of the Pressure Fluctuation: Part I," *Bull. of JSME*, **8**, 375 (1965a)
- Ishigai, S., M. Yamane, and K. Roko, "Measurement of Component Flows in a Vertical Two-Phase Flow by Making Use of the Pressure Fluctuation: Part II," *Bull. of JSME*, **8**, 383 (1965b)
- Jasper, J., "The Surface Tension of Pure Liquid Compounds," *J. Phys. Chem. Ref. Data*, **1**, 841(1972)
- Jenkins, G.M., and D.G. Watts, *Spectral Analysis and Its Applications*, Holden Day, San Francisco (1968)
- Kara, S., B. Kelkar, Y.T. Shah, and N.L. Carr, "Hydrodynamics and Axial Mixing in a Three-Phase Bubble Column," *Ind. Eng. Chem. Proc. Des. Dev.*, **21**, 584 (1982)
- Kato, Y., A. Nishiwaki, T. Fukuda, and S. Tanaka, "The Behavior of Suspended Solid Particles and Liquid in Bubble Columns," *J. Chem. Eng. Jap.*, **5**, 112 (1972)
- Kelkar, B.G., S.P. Godbole, M.F. Honath, Y.T. Shah, N.L. Carr, and W.D. Deckwer, "Effect of Addition of Alcohols on Gas Holdup and Backmixing in Bubble Columns," *AIChE J.*, **29**, 361 (1983)
- Kelkar, B.G., Y.T. Shah, and N.L. Carr, "Hydrodynamics and Axial Mixing in a Three-Phase Bubble Column," *Ind. Eng. Chem. Proc. Des. Dev.*, **23**, 308 (1984)
- Kim, S.D., C.G.J. Baker, and M.A. Bergougnou, "Bubble Characteristics in Three-Phase Fluidized Beds," *Chem. Eng. Sci.*, **32**, 1299 (1977)

- Kolbel, H., and M. Ralek, "The Fischer-Tropsch Synthesis in the Liquid Phase," *Catal. Rev. Sci. Eng.*, **21**, 225 (1980)
- Krambeck, F.J., A.A. Avidan, C.K. Lee, and M.N. Lo, "Predicting Fluid Bed Reactor Efficiency Using Adsorbing Gas Tracers," Paper Presented at AIChE Annual Meeting, Chicago, (1985)
- Kuo, J.C.W., "Two-Stage Process for Conversion of Synthesis Gas to High Quality Transportation Fuels," Final Report to the Department of Energy for Contract Number DE-AC22-83PC60019 (1985)
- Lassahn G.D., "Two-Phase Flow Velocity Measurements Using Radiation Intensity Correlation," *ISA Trans.*, **15**, 297 (1975)
- Ledakowicz, S., H. Nettelhoff, R. Kokuun, and W.D. Deckwer, "Kinetics of the Fischer-Tropsch Synthesis in Slurry Phase on Promoted Iron Catalyst," *Ind. Eng. Chem. Fundam.*, **23**, 510 (1984)
- Lee, C.H., *Dynamics of Bubble Size Distribution and Wall Pressure Fluctuations in Airlift Fermentors*, Masters Thesis, Kansas State University, Manhattan (1983)
- Lee, Y.H., Y.J. Kim, B.G. Kelkar, and C.B. Weinberger, "A Simple Digital Sensor for Dynamic Gas Holdup Measurements in Bubble Columns," *Ind. Eng. Chem. Fund.*, **24**, 105 (1985)
- Lin, P.Y., and T.J. Hanratty, "Detection of Slug Flow from Pressure Measurements," *Int. J. of Mult. Flow*, **13**, 13 (1987)
- Matsui, G., "Identification of Flow Regimes in Vertical Gas-Liquid Two-Phase Flow Using Differential Pressure Fluctuations," *Int. J. of Mult. Flow*, **10**, 711 (1984)
- Matsui, G., "Automatic Identification of Flow Regimes in Vertical Two-Phase Flow Using Differential Pressure Fluctuations," *Nucl. Eng. Des.*, **95**, 221 (1986)

- Miyazaki, K., K. Isogai, Y. Fujii-e, and T. Suita, "Measurement of Propagation Velocities of Pressure and Void By Cross Correlation Fluctuations in Nitrogen-Water Flow," *J. of Nucl. Sci. Tech.*, **10**, 323 (1973)
- Murray P., and L.S. Fan, "Axial Solids Distribution in Slurry Bubble Columns," *Ind. Eng. Res.*, **28**, 1697 (1989)
- O'Dowd, W., D.N. Smith, J.A. Ruether, and S.C. Saxena, "Gas and Solids Behavior in a Baffled and Unbaffled Slurry Bubble Column," *AIChE J.*, **33**, 1959 (1987)
- Orcutt, J.C., and B. H. Carpenter, "Bubble Coalescence and Simulation of Mass Transport and Chemical Reaction in Gas Fluidized Beds," *Chem. Eng. Sci.*, **26**, 1049 (1971)
- Ouyang C.J.P., and G.B. Tatterson, "The Effect of Distributors on Two-Phase and Three-Phase Flows in Vertical Columns," *Chem. Eng. Commun.*, **49**, 197 (1987)
- Parulekar, S.J., and Y.T. Shah, "Steady State Behavior of Gas-Liquid-Solid Fluidized Bed Reactors," *Chem. Eng. J.*, **20**, 21 (1980)
- Patel, S.A., *Investigation of Two-Phase Flow Structures in an Airlift Fermentor*, PhD Dissertation, Kansas State University, Manhattan (1985)
- Patel, S.A., J.G. Daly, and D.B. Bukur, "Holdup and Interfacial Area Measurements Using Dynamic Gas Disengagement," *AIChE J.*, **35**, 931 (1989)
- Patel, S.A., J.G. Daly, and D.B. Bukur, "Bubble-Size Distributions in Fischer-Tropsch Derived Waxes in Bubble Columns," *AIChE J.*, **36**, 93 (1990)
- Perry, and Chilton, *Chemical Engineers Handbook*, McGraw-Hill, New York (1983)
- Peter, S., and M. Weinert, "Über die Löslichkeit von H₂, CO, CO₂, and Wasserdampf in flüssigen Kohlenwasserstoffen," *Z. Physik. Chem.*, **5**, 114 (1955)

Petrick, M., and B.S. Swanson, "Radiation Attenuation Method of Measuring Density of a Two-Phase Fluid," *Rev. of Sci. Instr.*, **29**, 1079 (1958)

Quicker, G., and W.D. Deckwer, "A Further Note on Mass Transfer Limitations in the Fischer-Tropsch Slurry Process," *Chem. Eng. Sci.*, **36**, 1577 (1981)

Rabiger, N., "Die Auswirkung von Feststoffpartikeln auf den Gasgehalt in einem von oben begasteten Schlaufenreaktor," *Chem. Ing. Tech.*, **57**, 248 (1985)

Reilly, I.G., D.S. Scott, T. De Bruijn, A. Jain, and J. Piskorz, "A Correlation for Gas Holdup in Turbulent Coalescing Bubble Columns," *Can. J. Chem. Eng.*, **64**, 705 (1986)

Rodden, J.B., "Diffusion Coefficients for Several Dilute Solutes in n-Eicosane, n-Octacosane, and Fischer-Tropsch Wax," PhD Dissertation, Texas A&M University (1988)

Rodden, J.B., C. Erkey, and A. Akgerman, "Mutual Diffusion Coefficients for Several Dilute Solutes in n-Octacosane and the Solvent Density at 371-534 K," *J. Chem. Eng. Data*, **33**, 450 (1988)

Sada, E., H. Kumazawa, C. Lee, and T. Iguchi, "Gas Holdup and Mass Transfer Characteristics in a Three-Phase Bubble Column," *Ind. Eng. Chem. Proc. Des. Dev.*, **25**, 472 (1986)

Sanders, E., S. Ledakowicz, and W.D. Deckwer, "Fischer-Tropsch Synthesis in Bubble Column Slurry Reactors of Fe/K Catalyst," *Can. J. Chem. Eng.*, **64**, 133 (1986)

Sauer, T., and D.C. Hempel, "Fluid Dynamics and Mass Transfer in a Bubble Column with Suspended Particles," *Chem. Eng. Tech.*, **10**, 180 (1987)

Saxena, S.C., D. Patel, D.N. Smith, and J.A. Ruether, "An Assessment of Experimental Techniques for the Measurement of Bubble Size in a Bubble Slurry Reactor as Applied to Indirect Coal Liquefaction," *Chem. Eng. Commun.*, **63**, 87 (1988)

- Schumpe, A., and W.D. Deckwer, "Gas Holdups, Specific Interfacial Areas, and Mass Transfer Coefficients of Aerated Carboxymethyl Cellulose Solutions in a Bubble Column," *Ind. Eng. Chem. Proc. Des. Dev.*, **21**, 706 (1982)
- Schumpe, A., and A. Grund, "The Gas Disengagement Technique for Studying Gas Holdup Structure in a Bubble Column," *Can. J. Chem. Eng.*, **64**, 891 (1986)
- Seo, Y.C., and D. Gidaspo, "An X-Ray-Gamma-Ray Method of Measurement of Binary Solids Concentrations and Voids in Fluidized Beds," *Ind. Eng. Chem. Res.*, **26**, 1622 (1987)
- Shah, Y.T., B.G. Kelkar, S.P. Godbole, and W.D. Deckwer, "Design Parameter Estimations for Bubble Column Reactors," *AIChE J.*, **28**, 353 (1982)
- Shah, Y.T., S. Joseph, D.N. Smith, and J.A. Ruether, "On the Behavior of the Gas Phase in a Bubble Column with Ethanol-Water Mixtures," *Ind. Eng. Chem. Proc. Des. Dev.*, **24**, 1140 (1985)
- Smith, D.N., and J.A. Ruether, "Dispersed Solid Dynamics in a Slurry Bubble Column Reactor," *Chem. Eng. Sci.*, **40**, 741 (1985)
- Smith, J., K.M. Gupte, T.M. Leib, and J.W.C. Kuo, "Hydrodynamics Studies of Fischer-Tropsch Bubble Column Systems," Paper Presented at the AIChE Summer National Meeting, Philadelphia, (1984)
- Sriram, K., and R. Mann, "Dynamic Gas Disengagement: a New Technique for Assessing the Behavior of Bubble Columns," *Chem. Eng. Sci.*, **32**, 571 (1977)
- Taitel, Y., D. Bornea, and A.E. Dukler, "Modeling Flow Pattern Transitions for Steady Upward Gas-Liquid Flow in Vertical Tubes," *AIChE J.*, **27**, 1043 (1981)
- Thompson, G.J., M.L. Riekema, and A.G. Vickers, "Comparison of Fischer-Tropsch Reactor Systems," Final Report to the Department of Energy for Contract Number DE-AC01-78ET 10159 (1981)

- Tsao, T.R., "Results of LaPorte Liquid Phase Methanol PDU Unit," Proc. of Fourth DOE Contractors' Conference on Indirect Liquefaction, Washington, PA (1984)
- Vermeer, D.J., and R. Krishna, "Hydrodynamics and Mass Transfer in Bubble Columns Operating in the Churn-Turbulent Regime," *Ind. Eng. Chem. Proc. Des. Dev.*, **20**, 475 (1981)
- Weimer, A.W., D.C. Gyure, and D.E. Cough, "Application of a Gamma Radiation Density Gauge for Determining Hydrodynamic Properties of Fluidized Beds," *Powder Tech.*, **44**, 179 (1985)
- Ying D.H.S., R. Sivasobramanian, and E.N. Givens, "Gas/Slurry Flow in Coal Liquefaction Processes," Final Report to the Department of Energy for Contract Number Fe-14801-3 (1980)
- Zaidi, A., Y. Louisi, M. Ralek, and W.D. Deckwer, "Mass Transfer in the Liquid Phase Fischer-Tropsch Synthesis," *Ger. Chem. Eng.*, **2**, 94 (1979)
- Zheng, C., B. Yao, and Y. Feng, "Flow Regime Identification and Gas Holdup of Three-Phase Fluidized Systems," *Chem. Eng. Sci.*, **43**, 2195 (1988)
- Zigrand, D.J., and N.D. Sylvester, "An Explicit Equation for Particle Settling Velocities in Solid-Liquid Systems," *AIChE J.*, **27**, 1043 (1980)

IX. ACKNOWLEDGEMENT

We are grateful to Mike Noak and Randy Marek for their help with design and construction of experimental apparatus, and to Manne Ramakrishna for his technical assistance with the preparation of the final report. SASOL reactor wax was supplied by Sasol Technology Ltd. of South Africa, through Dr. Ben Jager.