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## Quantitative Tomographic Measurements of Opaque Multiphase Flows

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# Quantitative Tomographic Measurements of Opaque Multiphase Flows

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## Abstract

An electrical-impedance tomography (EIT) system has been developed for quantitative measurements of radial phase distribution profiles in two-phase and three-phase vertical column flows. The EIT system is described along with the computer algorithm used for reconstructing phase volume fraction profiles. EIT measurements were validated by comparison with a gamma-densitometry tomography (GDT) system. The EIT system was used to accurately measure average solid volume fractions up to 0.05 in solid-liquid flows, and radial gas volume fraction profiles in gas-liquid flows with gas volume fractions up to 0.15. In both flows, average phase volume fractions and radial volume fraction profiles from GDT and EIT were in good agreement. A minor modification to the formula used to relate conductivity data to phase volume fractions was found to improve agreement between the methods. GDT and EIT were then applied together to simultaneously measure the solid, liquid, and gas radial distributions within several vertical three-phase flows. For average solid volume fractions up to 0.30, the gas distribution for each gas flow rate was approximately independent of the amount of solids in the column. Measurements made with this EIT system demonstrate that EIT may be used successfully for noninvasive, quantitative measurements of dispersed multiphase flows.

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# Contents

<b>Nomenclature</b> .....	9
<b>1. Introduction</b> .....	14
<b>2. A Review of Vertical Multiphase Flow Studies</b> .....	17
2.1. Relevant Quantities in Vertical Multiphase Flows .....	17
2.2. Experimental Data and Correlations .....	19
2.3. Mathematical Multiphase Flow Models.....	29
2.4. Reactor Design and Scaleup Issues .....	36
<b>3. The Sandia/Michigan Electrical-Impedance Tomography (EIT) System</b> .....	39
3.1. EIT Theory .....	40
3.2. System Description .....	42
3.3. Validation of Reconstruction Algorithms .....	57
3.4. Selection of Electrode Geometry for Multiphase Flow Measurements .....	66
3.5. Summary .....	67
<b>4. Evaluation of the Sandia/Michigan EIT System in Two-Phase Flows</b> .....	69
4.1. The Sandia GDT System.....	70
4.2. Solid-Liquid Experiments .....	73
4.3. Gas-Liquid Experiments .....	79
4.4. Conclusions .....	90
<b>5. Investigation of Three-Phase Flows with EIT</b> .....	91
5.1. Experimental Setup .....	91
5.2. Calculation of Phase Volume Fraction Profiles .....	100
5.3. Results and Discussion.....	103
5.4. Conclusions .....	113
<b>6. Conclusions</b> .....	116
<b>References</b> .....	119
<b>Appendix A - Circuit Diagrams of the Sandia/Michigan EIT System</b> .....	124

<b>Appendix B</b> - EIT Data Acquisition Code FASTEIT . BAS .....	134
<b>Appendix C</b> - EIT Data Acquisition Code SLOWEIT . BAS.....	146
<b>Appendix D</b> - EIT Data Acquisition Subroutines .....	156
<b>Appendix E</b> - EIT Reconstruction Code FEMEIT . F .....	172
<b>Appendix F</b> - EIT Reconstruction Code EITAXI . F .....	187
<b>Appendix G</b> - Supplementary EIT Code EITFUN . F.....	196
<b>Appendix H</b> - Supplementary EIT Code EITFUL . F.....	201
<b>Appendix I</b> - GDT Reconstruction Code GDTAXI . F .....	204
<b>Appendix J</b> - Three-Phase Reconstruction Code GDTEIT . F .....	214
<b>Appendix K</b> - Phase Volume Fraction Profiles.....	218

**Figures**

2.1 Vertical gas-liquid flow regimes of interest in bubble-column hydrodynamics....	20
2.2 Flow regime map for vertical air-water bubble columns .....	21
2.3 Conceptual diagram of the modeling process for bubble-column reactors .....	37
3.1 Conceptual diagram of an EIT system applied to a circular domain .....	40
3.2 Block diagram of the Sandia/Michigan EIT system .....	43
3.3 Photograph of the Sandia/Michigan EIT system .....	43
3.4 EIT electrode arrays .....	46
3.5 Flow chart of EIT reconstruction algorithm .....	48
3.6 Basis functions used in EIT quartic algorithm .....	51
3.7 Region of parameter space in which conductivity is nonnegative at all radial locations .....	52
3.8 Discrete points in parameter space at which FIDAP computations were performed .....	53
3.9 FIDAP mesh on which fundamental voltage solutions were computed .....	54
3.10 Plots of fundamental voltage $V_7$ along selected curves .....	56
3.11 Finite-element mesh used by FIDAP in validation tests and synthetic benchmark conductivity field .....	58
3.12 Finite-element mesh used by FEMEIT in validation tests and reconstructed conductivity field .....	59

3.13	Conductivity reconstructions for two-dimensional validation tests with inclusions .....	61
3.14	Comparison of effective conductivities computed by FIDAP with predictions from the Maxwell-Hewitt relations .....	63
4.1	The Sandia GDT system and the transparent bubble column used in gas-liquid experiments .....	71
4.2	Conceptual diagram of the Sandia GDT system as viewed from above .....	72
4.3	Block diagram of the Sandia GDT system .....	72
4.4	Schematic of test geometry for the solid-liquid experiments .....	74
4.5	Photograph of the testbed for polystyrene-water solid-liquid experiments .....	75
4.6	Photograph of polystyrene particles used as the solid phase .....	76
4.7	Photograph of flow conditions during solid-liquid experiments with $\bar{\epsilon}_s^{NOM} = 0.01$ .....	77
4.8	Solid volume fractions measured by EIT in polystyrene-water solid-liquid mixtures .....	78
4.9	Comparison of testbed-averaged solid volume fractions measured by EIT and GDT in glass-water mixtures .....	79
4.10	Experimental setup for EIT validation experiments in the Lexan bubble column.	80
4.11	Typical cartridge heater used to maintain constant temperature within bubble-column flows .....	81
4.12	Sparger designs used in the unsuccessful homogeneous bubbly flow experiments	82
4.13	Ring sparger used in churn-turbulent flow experiments .....	82
4.14	Churn-turbulent flow conditions in the transparent bubble column at minimum and maximum volumetric flow rates.....	83
4.15	Comparisons of symmetric radial gas volume fraction profiles from GDT and EIT	85
4.16	Comparison of cross-sectionally-averaged gas volume fractions measured by GDT and EIT .....	86
4.17	Impedance-based bulk void fraction meter used to investigate fluctuations in gas volume fraction .....	86
4.18	Concept of the modified Maxwell-Hewitt relation .....	88
4.19	GDT and EIT reconstructions using quadratic and quartic profiles .....	89
5.1	Photograph and size distribution of large polystyrene beads .....	93
5.2	Photograph and size distribution of medium polystyrene beads .....	94
5.3	Photograph and size distribution of medium glass beads .....	95
5.4	Photograph and size distribution of small glass beads .....	96
5.5	Photographs of flow conditions in three-phase, polystyrene-air-water flows in the transparent bubble column .....	99
5.6	Phase volume fraction profiles determined from EIT and GDT reconstructions for a superficial gas velocity of $U_G = 8.8$ cm/s and a solid phase of 400 $\mu$ m polystyrene particles .....	104



5.7	Phase volume fraction profiles determined from EIT and GDT reconstructions for a superficial gas velocity of $U_G = 17.5$ cm/s and a solid phase of 200- $\mu$ m glass particles .....	105
5.8	Average gas volume fractions for large polystyrene beads .....	106
5.9	Average gas volume fractions for medium polystyrene beads .....	106
5.10	Average gas volume fractions for medium glass beads .....	107
5.11	Average gas volume fractions for small glass beads .....	107
5.12	Average gas volume fractions for all two-phase and three-phase experiments to date .....	108
5.13	Dependence of average gas volume fraction on nominal solid volume fraction for all three-phase experiments involving glass particles .....	109
5.14	Dependence of average gas volume fraction on nominal solid volume fraction for all three-phase experiments involving polystyrene particles .....	109
5.15	Comparison of gas profiles computed from GDT attenuation data taken above and below the EIT electrode ring for $\bar{\epsilon}_s^{NOM} = 0.22$ .....	110
5.16	Dependence of the ratio $\bar{\epsilon}_s / (\bar{\epsilon}_s + \bar{\epsilon}_L)$ on superficial gas velocity, calculated using the original Maxwell-Hewitt relation .....	112
5.17	Dependence of the ratio $\bar{\epsilon}_s / (\bar{\epsilon}_s + \bar{\epsilon}_L)$ on superficial gas velocity, calculated using the modified Maxwell-Hewitt relation .....	112
5.18	Comparison of measured and predicted average gas volume fractions in three-phase flows involving glass particles .....	114
5.19	Comparison of measured and predicted average gas volume fractions in three-phase flows involving polystyrene particles .....	114

## Tables

3.1	Effect of FEMEIT mesh refinement on reconstruction accuracy of a uniform domain.....	58
3.2	Effect of FEMEIT mesh refinement on reconstruction accuracy of a synthetic conductivity distribution .....	59
3.3	Comparison of actual and reconstructed geometries of insulating inclusions in two-dimensional validation tests with strip electrodes .....	60
3.4	Fundamental voltage solutions for 16 strip electrodes in the transparent bubble column .....	61
3.5	Comparison of actual and reconstructed geometries of insulating inclusions in three-dimensional validation tests with disk electrodes .....	62
3.6	Fundamental voltage solutions used in uncertainty analysis .....	66
3.7	Conductivity parameter values resulting from voltages in Table 3.6 .....	66
4.1	Comparison of differences between EIT and GDT measurements with temporal fluctuations in gas volume fraction .....	87
5.1	Properties of the materials used in the three-phase experiments .....	92
5.2	Three-phase experimental conditions analyzed with the EIT/GDT system .....	98